

Scalable Model Selection for Belief Networks

Supplemental Materials

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1 Derivation of Minibatch gFIC in (7)

We first note that an unbiased estimator for (5) is

$$\begin{aligned}
 \widehat{\text{gFIC}}_{\text{SBN}} = & \max_q \mathbb{E}_q \left[-\frac{M}{2} \sum_j \ln \left(\frac{N_{T+1}}{N_{\text{mini}}} \sum_{i=1}^{N_{\text{mini}}} h_{i+N_T, j} \right) \right. \\
 & \left. + \frac{N_{T+1}}{N_{\text{mini}}} \sum_{i=1}^{N_{\text{mini}}} \ln \frac{p(\mathbf{v}_{i+N_T}, \mathbf{h}_{i+N_T} | \hat{\boldsymbol{\theta}})}{q(\mathbf{h}_{i+N_T} | \phi)} + \frac{MJ - D_{\boldsymbol{\theta}}}{2} \ln N_{T+1} \right] \quad (\text{A1})
 \end{aligned}$$

Simplifying and ignoring constant terms in (A1) leads to $\widetilde{\text{gFIC}}_{\text{SBN}}$ in (7) of the main text.

2 Additional Results

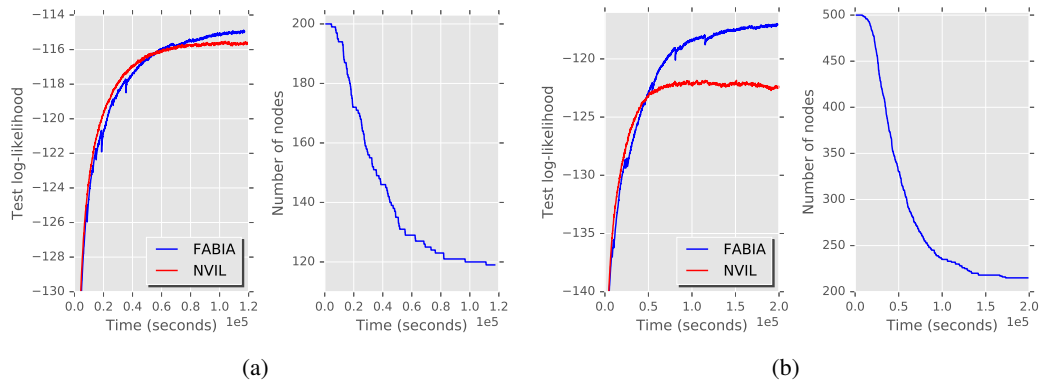


Figure A1: Test log-likelihood and the number of nodes in FABIA, as a function of CPU time on the MNIST dataset, for an SBN with initial size as (a) 200 (b) 500.

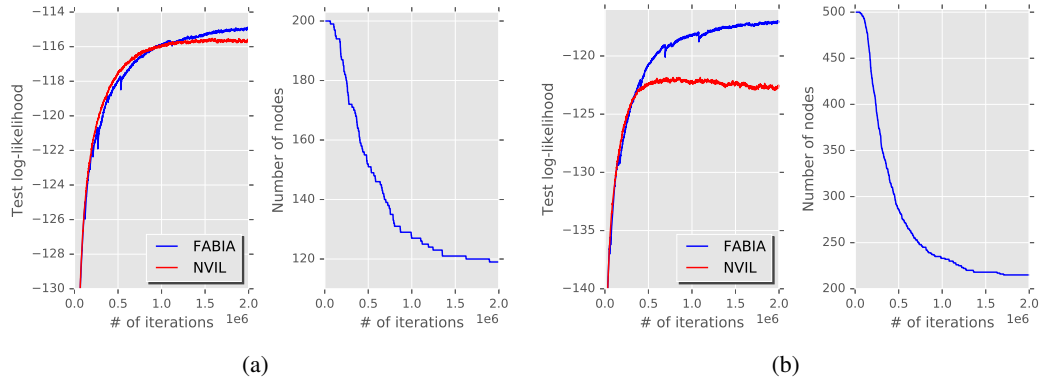


Figure A2: Test log-likelihood and the number of nodes in FABIA, as a function of the number of iterations on the MNIST dataset, for an SBN with initial size as (a) 200 (b) 500.

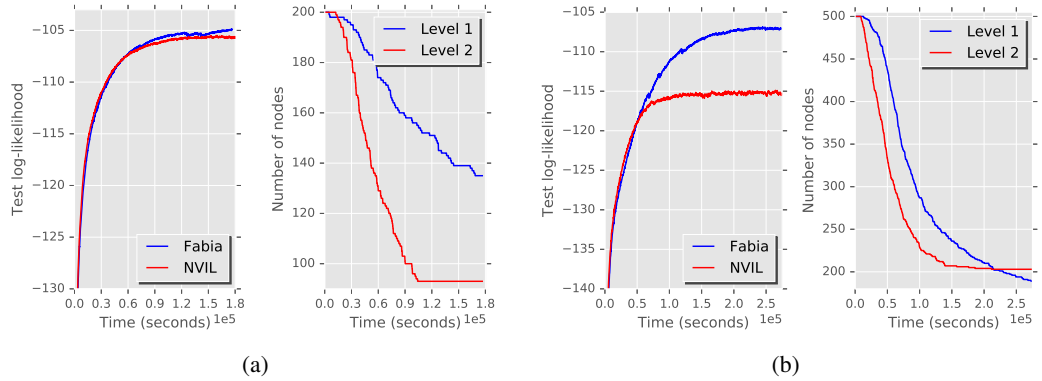


Figure A3: Test log-likelihood and the number of nodes in FABIA, as a function of CPU time on the MNIST dataset, for an SBN with initial size as (a) 200-200 (b) 500-500.

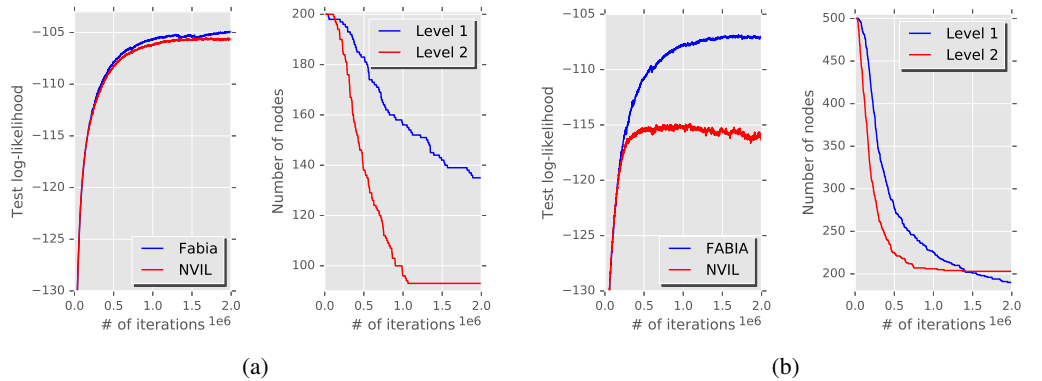


Figure A4: Test log-likelihood and the number of nodes in FABIA, as a function of the number of iterations on the MNIST dataset, for an SBN with initial size as (a) 200-200 (b) 500-500.

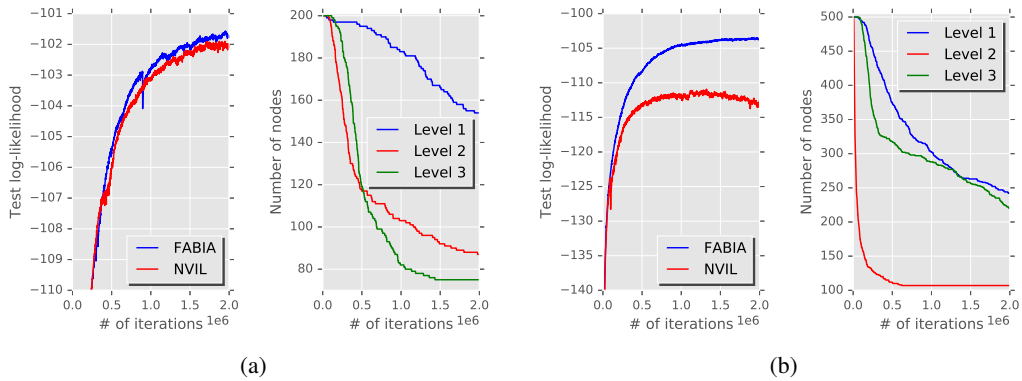


Figure A5: Test log-likelihood and the number of nodes in FABIA, as a function of the number of iterations on the MNIST dataset, for an SBN with initial size as (a) 200-200-200 (b) 500-500-500.

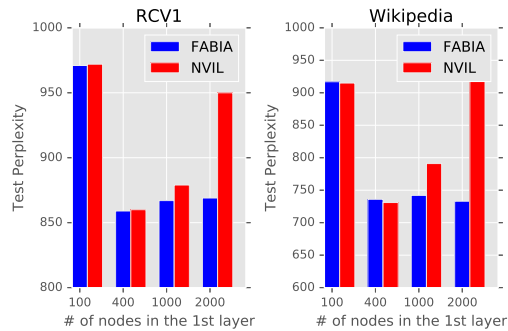


Figure A6: Test perplexities as a function of number of nodes in the first layer, in the three-layer case.

Table 1: Test perplexities and model size on the benchmarks, for NVIL and FABIA with three layers. FABIA starts from a model initialized with 400 hidden units in each layer.

	RCV1		Wikipedia	
	Size	Perplexity	Size	Perplexity
NVIL	400-400-400	859	400-400-400	731
FABIA	398-46-10	860	400-36-9	737